## Instructions

This exam contains 15 pages (including this cover page) and 28 questions. It is out of 100 points.

You have 50 minutes to complete the examination. As a courtesy to your classmates, we ask that you not leave during the last fifteen minutes.

For this exam, you have been given a separate scantron answer sheet to fill in your responses. We scan this into Gradescope so color in the bubble without going outside of the lines.

It is OK to write on your test pages.
It is NOT OK to write anything on your scantron answer sheet except for your name, computing ID, signature, and coloring in your bubbles (small circles) to answer the questions.

You may assume all questions on this test are single-select unless otherwise indicated.
You may not use a calculator or notes.
The next page contains reference material which you are welcome to refer to during the test if you would like.

## Our Example ISA

This is the same ISA used in HW03 and HW04, but presented to fit onto one printed page.
Each instruction is one or two bytes, with the meaning of those bytes being:

| 7 |  | 5 | 3 | 1 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | icode | a | b |  |

byte at pc


Not all instructions have the second byte; those that do describe it below as the byte "at pc +1 ".
In the table below rA means "the value stored in register number a" and rB means "the value stored in register number b."

| icode | b | Behavior | add to pc |
| :---: | :---: | :---: | :---: |
| 0 |  | $r A=r B$ | 1 |
| 1 |  | $r A+=r B$ | 1 |
| 2 |  | $r A \&=r B$ | 1 |
| 3 |  | $r A=r e a d$ from memory at address $r B$ | 1 |
| 4 |  | write $r A$ to memory at address $r B$ | 1 |
| 5 | 0 | $r A=\sim r A$ | 1 |
| 5 | 1 | $r A=-r A$ | 1 |
| 5 | 2 | $r A=!r A$ | 1 |
| 5 | 3 | $r A=p c$ | 1 |
| 6 | 0 | $r A=r e a d$ from memory at $\mathrm{pc}+1$ | 2 |
| 6 | 1 | $r A+=$ read from memory at $p c+1$ | 2 |
| 6 | 2 | $r A \&=$ read from memory at $p c+1$ | 2 |
| 6 | 3 |  | 2 |
| 7 |  | if $\mathrm{rA}<=0$, set $\mathrm{pc}=r \mathrm{~B}$ | N/A |
| 7 |  | if $r A>0$, do nothing | 1 |

If the first bit of the byte at pc is 1 instead of 0 , the above text does not define what the instruction means, but some other source (such as a question on this exam) might. If it has no defined meaning either here or elsewhere, leave the pc and all other registers and memory values unchanged.

1 Logic Gates \& Boolean Algebra

1. (4 points) Given input A , what is the output Y of the following circuit?

(A) A
(B) $\sim \mathrm{A}$
(C) GND
(D) $V_{D D}$

Solution: (A) A
2. (6 points) Which of the following representations are equivalent to A NOR B? Select all that apply.
(A)

(C)

(E)

(B) $Y=\sim(A \& B)$
(D) $\mathrm{Y}=\sim \mathrm{A} \mid \sim \mathrm{B}$
(F) $Y=\sim(A \mid B)$

Solution: (A) This is a circuit representation of $\sim$ A $\& \sim B$, which is the same as $\sim(A \mid B)$ = A NOR B.
(E) nor gate
(F) ~ (A | B)
partial credit:
+2 points per correct selection
-2 points per incorrect selection (can earn no less than 0 points)

Without any simplification, the logic expression $Y=(A \wedge B) \& \sim(B \& C)$ is to be implemented in hardware using the skeleton shown below.

3. (2 points) Which gate should be placed in Box 1?
(A)

(B)

(C)

(D)


Solution: (B) xor gate
4. (2 points) Which gate should be placed in Box 2?
(A)

(B)

(C)

(D)


Solution: (A) nand gate
5. (2 points) Which gate should be placed in Box 3?
(A)

(B)

(C)

(D)


Solution: (C) and gate

## 2 Number Representations

6. (4 points) The two's complement number representation has a "weird" number that has no positive counterpart because it is its own two's complement. Which of the following is the "weird" number in 4-bit two's complement?
(A) 0 b 0111
(B) 0 b1000
(C) 0 b1111
(D) 0 b 0000

Solution: (B) 0b1000
2 points for (D) 0 b0000 since it is technically its own two's complement if carry out is ignored
7. (2 points) True or False: When using 4 bits to represent numbers, the bit representation of 5 is the same in two's complement as in the unsigned representation.
(A) True
(B) False

Solution: (A)
8. (5 points) While reviewing code on a 32-bit system, you come across the following lines of code:

```
X = 0x1234
mask = ~0x0F
extraction = X & mask
print(extraction)
```

What is the output in hex?
(A) $0 \times 1234$
(B) $0 \times 0034$
(C) $0 \times 0030$
(D) $0 \times 1230$
(E) $0 \times 123 \mathrm{~F}$
(F) $0 \times$ FFF4
(G) $0 \times 0000$

Solution: (D).
9. (6 points) If a little-Endian x86 computer were to read the 32 -bit number $0 \times 12345678$ from a big-Endian network without accounting for the difference in Endian-ness, how would the computer interpret the number?

Solution: $0 \times 78563412$

## 3 IEEE Floating Point

Write the following binary number as a 16 -bit IEEE-style floating-point number assuming a 4 -bit exponent value:
$-100100.11010001$
10. (3 points) What should the sign bit be set to?

Solution: 0b1
11. (5 points) How would the 4 -bit exponent be represented in binary?

## Solution: 0b1100

12. (5 points) How would the mantissa be represented in binary?

Solution: 0b00100110100

## 4 Circuits \& Registers

13. (5 points) Consider the following diagram (note this is not our standard set-up for writing to a register file).


What is the value in each register after the next rising CLK edge?
(A) $\mathrm{R} 0=0 \mathrm{x} 0, \mathrm{R} 1=0 \mathrm{x} 0, \mathrm{R} 2=0 \mathrm{x} 5, \mathrm{R} 3=0 \mathrm{x} 0$
(D) $\mathrm{R} 0=0 \mathrm{xA}, \mathrm{R} 1=0 \mathrm{xB}, \mathrm{R} 2=0 \mathrm{x} 5, \mathrm{R} 3=0 \mathrm{xD}$
(B) $\mathrm{R} 0=0 \mathrm{xA}, \mathrm{R} 1=0 \mathrm{xB}, \mathrm{R} 2=0 \mathrm{xC}, \mathrm{R} 3=0 \mathrm{xD}$
(E) $\mathrm{R} 0=0 \mathrm{x} 1, \mathrm{R} 1=0 \mathrm{x} 1, \mathrm{R} 2=0 \mathrm{x} 1, \mathrm{R} 3=0 \mathrm{x} 1$
(C) $\mathrm{R} 0=0 \mathrm{x} 0, \mathrm{R} 1=0 \mathrm{x} 0, \mathrm{R} 2=0 \mathrm{x} 0, \mathrm{R} 3=0 \mathrm{x} 0$
(F) $\mathrm{R} 0=0 \mathrm{x} 1, \mathrm{R} 1=0 \mathrm{x} 1, \mathrm{R} 2=0 \mathrm{x} 5, \mathrm{R} 3=0 \mathrm{x} 1$

Solution: (A)

14. (5 points) Given the timing diagram for a positive edge-triggered D flip-flop shown above, what is the value of the output Q at times $\mathrm{A}, \mathrm{B}$, and C ?
(A) $\mathrm{A}: \mathrm{Q}=0, \mathrm{~B}: \mathrm{Q}=0, \mathrm{C}: \mathrm{Q}=0$
(E) $\mathrm{A}: \mathrm{Q}=1, \mathrm{~B}: \mathrm{Q}=0, \mathrm{C}: \mathrm{Q}=0$
(B) $\mathrm{A}: \mathrm{Q}=0, \mathrm{~B}: \mathrm{Q}=0, \mathrm{C}: \mathrm{Q}=1$
(F) $\mathrm{A}: \mathrm{Q}=1, \mathrm{~B}: \mathrm{Q}=0, \mathrm{C}: \mathrm{Q}=1$
(C) $\mathrm{A}: \mathrm{Q}=0, \mathrm{~B}: \mathrm{Q}=1, \mathrm{C}: \mathrm{Q}=0$
(G) $\mathrm{A}: \mathrm{Q}=1, \mathrm{~B}: \mathrm{Q}=1, \mathrm{C}: \mathrm{Q}=0$
(D) $\mathrm{A}: \mathrm{Q}=0, \mathrm{~B}: \mathrm{Q}=1, \mathrm{C}: \mathrm{Q}=1$
(H) $\mathrm{A}: \mathrm{Q}=1, \mathrm{~B}: \mathrm{Q}=1, \mathrm{C}: \mathrm{Q}=1$

Solution: (C)
partial credit:
1 point for answers: (B), (E), and (H)
2 points for answers: (A), (D), and (G)

The questions on this page consider the register file pictured below, with the inputs and outputs as defined in-class:

- A1 and A2 are the two addresses to read from
- A3 is the address to write to
- WE3 is the write enable
- WD3 is the write data input
- RD1 and RD2 are the two read outputs


You may assume that this register file is implemented using positive edge-triggered $\mathbf{D}$ flip-flops.
Select the inputs below required to write the number 0x45 to register number 0x02. If an input's value does not matter, match it to "any value."
15. (2 points) A1:
(A) 1
(B) 0
(C) $0 \times 45$
(D) $0 x 02$
(E) Rising Edge
(F) Falling Edge
(G) Any value

Solution: (G)
16. (2 points) A2:
(A) 1
(B) 0
(C) $0 x 45$
(D) 0 x 02
(E) Rising Edge
(F) Falling Edge
(G) Any value

Solution: (G)
17. (2 points) A3:
(A) 1
(B) 0
(C) $0 \times 45$
(D) $0 x 02$
(E) Rising Edge
(F) Falling Edge
(G) Any value

Solution: (D)
18. (2 points) WD3:
(A) 1
(B) 0
(C) $0 \times 45$
(D) 0 x 02
(E) Rising Edge
(F) Falling Edge
(G) Any value

Solution: (C)
19. (2 points) WE3:
(A) 1
(B) 0
(C) $0 \times 45$
(D) $0 \times 02$
(E) Rising Edge
(F) Falling Edge
(G) Any value

Solution: (A)
20. (2 points) CLK:
(A) 1
(B) 0
(C) $0 \times 45$
(D) $0 x 02$
(E) Rising Edge
(F) Falling Edge
(G) Any value

Solution: (E)
1 point for (A) 1

## 5 Toy ISA

Questions 21-23 consider the following block of memory.

|  | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{D}$ | $\mathbf{D}$ | $\mathbf{E}$ | $\mathbf{F}$ |  |  |  |  |  |  |  |  |  |  |
| $\mathbf{0 0}$ | 60 | 18 | 64 | 20 | 68 | 22 | 6 C | 24 | 36 | 00 | 01 | 02 | 03 |
| 04 | 05 | 06 |  |  |  |  |  |  |  |  |  |  |  |
| $\mathbf{1 0}$ | 07 | 08 | 09 | OA | OB | OC | OD | 0 E | OF | 10 | 11 | 12 | 13 |
| $\mathbf{2 0}$ | 17 | 18 | 19 | 1 A | 1 B | 1 C | 1 D | 1 E | 1 F | 20 | 21 | 22 | 23 |

The first 8 bytes of memory load values into the registers such that the state of the machine is

- $\mathrm{pc}=0 \times 08$
- r0 = 0x18
- $r 1=0 \times 20$
- $r 2=0 \times 22$
- $r 3=0 \times 24$

The following questions concern the next instruction (boxed above), which will impact the pc and one of the registers.
21. (4 points) What is the value of the pc after the command executes?

Solution: (A) $0 \times 9$
22. (2 points) Which register will change value?
(A) r 0
(B) $r 1$
(C) $r 2$
(D) r 3

Solution: (B) r1
23. (6 points) What will the new value stored be in that register be?

## Solution: $0 \times 19$

24. (5 points) Select the instruction below that stores the value of the program counter in register 2.
(A) 01011011
(B) 00111011
(C) $0 \quad 110 \quad 1011$
(D) $0 \quad 101 \quad 1111$
(E) $0 \quad 101 \quad 1110$

Solution: (A)
25. (5 points) Using the example ISA, which of the following lines of code loads the value $0 \times 12$ into register 3?
(A) $0 \times 0 \mathrm{~A} 0 \times 12$
(B) $0 \times 030 \times 12$
(C) $0 \times 6 \mathrm{C} 0 \times 12$
(D) $0 \times 630 \times 12$
(E) $0 \times 6 \mathrm{D} 0 \times 12$

Solution: (C)

## 6 Control signals

Consider the following diagram, which is a subset of our toy ISA architecture.


The following three questions ask you to determine the control signals $\mathrm{C}_{0}, \mathrm{C}_{4}$, and $\mathrm{C}_{6}$ when icode $=6$ and $b=0$.

| icode | b | Behavior | add to pc |
| :---: | :--- | :--- | :---: |
| 6 | 0 | $\mathrm{rA}=$ read from memory at $\mathrm{pc}+1$ | 2 |

26. (3 points) What is $\mathrm{C}_{0}$ ?
(A) 0
(B) 1
(C) Does not matter

Solution: (B)
27. (4 points) What is $\mathrm{C}_{4}$ ?
(A) 0
(B) 1
(C) 2
(D) 3
(E) Does not matter

Solution: (D)
28. (3 points) What is $\mathrm{C}_{6}$ ?
(A) 0
(B) 1
(C) Does not matter

Solution: (C)

